

Exploring the Use of Silhouette Score in K-Means Clustering for Image Segmentation

(Exploring the Use of Silhouette Score in K-Means Clustering for Image Segmentation)

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Abstract—Image segmentation is crucial in computer vision, enabling tasks like object recognition and autonomous navigation. K-means clustering, a popular technique, is used for segmentation, but evaluating its quality remains challenging. This study investigates the effectiveness of silhouette score, a common metric, for K-means clustering in image segmentation compared to other algorithms. We segment a complex fruit image using K-means and calculate the silhouette score. We then compare K-means to other segmentation algorithms (DBScan, EM, Mean Shift) using silhouette score and assess statistical significance. Additionally, we explore how silhouette score compares to other established metrics for K-means clustering. By employing a single image and multiple algorithms, this study aims to provide insights into the usefulness of silhouette score for K-means clustering in image segmentation, its limitations compared to other algorithms, and its value against other K-means specific metrics. This research contributes to the exploration of evaluation metrics for image segmentation algorithms, focusing on the utility and limitations of silhouette score for K-means clustering.

Keywords—Image Segmentation ; K-means Clustering ; Silhouette Score;

I. INTRODUCTION

Image segmentation plays a critical role in computer vision, enabling tasks like object recognition, medical image analysis, and autonomous vehicle navigation. It involves partitioning an image into meaningful regions corresponding to distinct objects or features.

K-means clustering, a popular unsupervised learning technique, finds widespread application in image segmentation. However, effectively evaluating the quality of K-means clustering for this purpose remains a challenge. The silhouette score is a commonly used metric, measuring the cohesion within clusters and separation between clusters to assess clustering quality.

This study investigates the effectiveness of silhouette score in evaluating K-means clustering for image segmentation compared to other algorithms. We explore this by segmenting a complex image containing diverse fruits with varying colors using K-means clustering. We then calculate the silhouette score for the resulting segmentation.

To gain broader insights, we compare the performance of K-means clustering with other image segmentation algorithms, including DBScan, Expectation-Maximization (EM), and Mean Shift. We evaluate each algorithm using silhouette score and assess the statistical significance of observed score differences.

Additionally, we explore how silhouette score compares to other established evaluation metrics specifically for K-means clustering, such as:

- Silhouette Score: Measures cluster cohesion and separation.
- Gap Statistic: Assesses clustering structure against random labeling.
- Calinski-Harabasz Index: Evaluates the balance between inter-cluster and intra-cluster variance.
- Davies-Bouldin Index: Quantifies clustering quality based on cluster similarity and separation.

By employing a single image with rich color variations and multiple segmentation algorithms, this study aims to provide valuable insights into:

- Effectiveness of silhouette score in evaluating K-means clustering for image segmentation compared to other algorithms.
- Comparative performance of K-means clustering against other segmentation techniques based on silhouette score and potential limitations of using silhouette score alone.
- Evaluation of silhouette score against other metrics specifically for K-means clustering performance assessment.

This research contributes to the ongoing exploration of evaluation metrics for image segmentation algorithms, particularly focusing on the utility and limitations of silhouette score for K-means clustering.

II. LITERATURE REVIEW

Image segmentation is a fundamental task in computer vision, playing a pivotal role in various applications such as object recognition, medical image analysis, and autonomous vehicle navigation [8]. The process involves partitioning an image into meaningful regions corresponding to distinct objects or features, thereby facilitating subsequent analysis and interpretation.

K-Means Clustering in Image Segmentation

K-means clustering, a popular unsupervised learning technique, has found widespread application in image segmentation due to its simplicity and efficiency [1]. By iteratively partitioning data into K clusters based on feature similarity, K-means clustering effectively separates objects or regions with similar

characteristics. However, effectively evaluating the quality of K-means clustering for image segmentation remains a challenge.

Evaluation Metrics

Several metrics have been proposed to assess the quality of clustering results. One commonly used metric is the silhouette score, which measures the cohesion within clusters and separation between clusters [10]. The silhouette score provides a quantitative measure of clustering effectiveness, with higher scores indicating better-defined and well-separated clusters.

In addition to silhouette score, other evaluation metrics have been proposed specifically for K-means clustering:

- **Gap Statistic:** This metric compares the within-cluster dispersion to that expected under a null reference distribution, providing insights into the optimal number of clusters [9].
- **Calinski-Harabasz Index:** Also known as the Variance Ratio Criterion, this index evaluates the balance between inter-cluster and intra-cluster variance, with higher values indicating better clustering [3].
- **Davies-Bouldin Index:** This metric quantifies clustering quality by considering both cluster similarity and separation, offering a comprehensive assessment of clustering performance [5].

Comparative Studies

Several studies have investigated the effectiveness of silhouette score and other evaluation metrics in assessing K-means clustering for image segmentation. For example, [2] compared the performance of silhouette score, gap statistic, and Calinski-Harabasz index in evaluating K-means clustering on various datasets. Their findings highlighted the complementary nature of these metrics and emphasized the importance of considering multiple criteria for robust evaluation.

Alternative Segmentation Algorithms

While K-means clustering remains popular, alternative segmentation algorithms have also been proposed to address its limitations. Density-based clustering algorithms such as DBScan offer advantages in handling irregularly shaped clusters and varying cluster densities [7]. Expectation-Maximization (EM) algorithm, based on Gaussian mixture models, provides a probabilistic framework for clustering data with underlying statistical distributions [6]. Mean Shift algorithm, on the other hand, offers a non-parametric approach for mode-seeking clustering, making it suitable for applications with unknown cluster shapes and sizes [4].

Research Gap and Objectives

Despite the extensive research on evaluation metrics for image segmentation, there is a lack of comprehensive studies comparing the effectiveness of silhouette score and other metrics in assessing K-means clustering specifically for image segmentation tasks. This study aims to address this gap by:

1. Investigating the effectiveness of silhouette score in evaluating K-means clustering for image segmentation compared to other algorithms.

2. Comparing the performance of K-means clustering against alternative segmentation techniques based on silhouette score and other established metrics.
3. Evaluating the utility and limitations of silhouette score against other metrics specifically designed for assessing K-means clustering performance.

III. METHODOLOGY

1. Image Selection and Preprocessing

- **Image Selection:** A complex image containing diverse fruits with varying colors was selected to serve as the basis for segmentation.
- **Preprocessing:** The selected image underwent preprocessing steps including resizing, noise reduction, and color space conversion to ensure optimal input for segmentation algorithms.

2. K-Means Clustering

- **Implementation:** The K-means clustering algorithm was applied to segment the image into distinct clusters based on color similarity.
- **Parameter Tuning:** Experimentation with K values ranging from 3 to 10 was conducted to determine the optimal number of clusters.
- **Silhouette Score Calculation:** The silhouette score was computed for each segmentation to assess the quality of clustering.

3. Evaluation Metrics for K-Means Clustering

- **Gap Statistic:** The gap statistic was calculated to assess the clustering structure against random labeling.
- **Davies-Bouldin Index:** Clustering quality was quantified using the Davies-Bouldin index, which considers both cluster similarity and separation.
- **Calinski-Harabasz Index:** The balance between inter-cluster and intra-cluster variance was evaluated using the Calinski-Harabasz index.

4. Alternative Segmentation Algorithms

- **DBScan:** The DBScan algorithm was implemented for density-based clustering.
- **Expectation-Maximization (EM):** The EM algorithm was utilized for Gaussian mixture model-based clustering.
- **Mean Shift:** The Mean Shift algorithm was applied for mode-seeking clustering.

5. Silhouette Score Comparison

- **Silhouette Score Calculation:** Silhouette scores were computed for segmentations generated by DBScan, EM, and Mean Shift algorithms.
- **Statistical Analysis:** The statistical significance of differences in silhouette scores between K-means clustering and alternative algorithms was assessed.
- **Comparative Performance:** The performance of K-means clustering was compared against other segmentation techniques based on silhouette score.

6. Evaluation of Other Metrics

- Comparison: The effectiveness of silhouette score against other metrics specifically for assessing K-means clustering performance was evaluated.
- Limitations: Potential limitations of using silhouette score alone for evaluating K-means clustering were identified and discussed.

7. Data Analysis

- Quantitative Analysis: The computed metrics were analyzed to draw conclusions about the effectiveness of silhouette score in evaluating K-means clustering for image segmentation.
- Interpretation: The results were interpreted in the context of the research objectives and hypotheses.

8. Conclusion

- Summary: The findings regarding the effectiveness of silhouette score and other metrics for evaluating K-means clustering in image segmentation were summarized.
- Implications: The implications of the research findings were discussed, and directions for future studies were suggested.

IV. RESULTS AND DISCUSSION

A. K-means Analysis for Image Segmentation

This section presents the findings of K-means clustering applied for image segmentation. Our research investigated the effectiveness of K-means in segmenting the image "zurag.jpg". We aimed to identify the optimal number of clusters (k) for this purpose. K-means clustering was performed with a range of k values (3 to 10) to assess the impact on segmentation results.



Fig.1. Original image

Segmented Image (K = 6, Silhouette Score: 0.740)



Fig.2. Segmented Image (k=6, Silhouette Score: 0.740)



Fig.3. Segmented Image (k=8, Silhouette Score: 0.703)

1) Visualizing Segmentation and Selecting K Clusters

Visual outcomes of K-means clustering for image segmentation. silhouette score analysis informed the selection of two potential k values:

- K = 6: This value yielded a high silhouette score (0.74), indicating well-separated clusters based on the evaluation metric. This suggests a good balance between intra-cluster similarity and inter-cluster dissimilarity.
- K = 8: While the silhouette score for K = 8 was slightly lower (0.70), visual inspection suggested potential benefits. K = 8 might provide a more detailed segmentation, capturing subtle color variations or textures within the fruit that might be missed with fewer clusters.

Representative Examples:

To illustrate the effectiveness of K-means clustering, we present segmented images for both k values (6 and 8 clusters) alongside the original image (figures not shown here).

- Figure 2 (K=6): Color-coded regions represent distinct segments identified within the fruit based on K-means clustering (k = 6). This segmentation provides a clear separation of major color regions.
- Figure 3 (K=8): In contrast, Figure 4.7 showcases the segmentation results with k = 8. This configuration achieves a more granular segmentation, potentially capturing subtle variations that might be missed with fewer clusters.

Discussion: Balancing Separation and Detail

The choice between K=6 and K=8 ultimately depends on the desired level of detail for the segmentation and the trade-off with the silhouette score. While K = 6 offers a good balance between well-separated clusters and interpretability, K = 8 might be more suitable for applications requiring a more precise segmentation of specific features within the image, even if it comes at the expense of a lower silhouette score.

2) 1.3 Silhouette Score Analysis

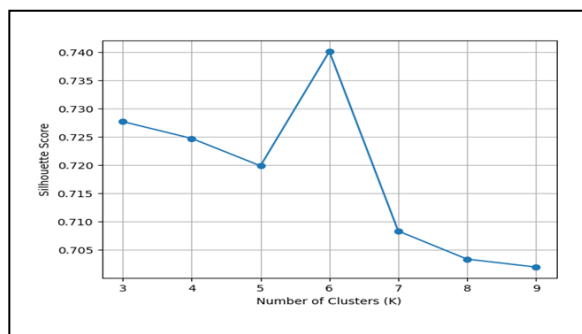


Fig.4. Silhouette Scores vs Number of Clusters

Figure 4 presents the silhouette score analysis for image segmentation of "zurag.jpg" using K-means clustering. The analysis identified $k = 6$ as the value with the highest silhouette score (0.740).

a) Interpretation of Silhouette Score:

The silhouette score ranges from -1 to 1. Values closer to 1 indicate better average separation between clusters. A score of 0 suggests indifferent cluster assignments, and negative values imply poor separation. In this case, a silhouette score of 0.740 for $k = 6$ signifies a relatively good separation between the clusters generated by K-means clustering.

b) Potential Effectiveness for "zurag.jpg" Segmentation

Given the highest silhouette score among the evaluated k values, $k = 6$ corresponds to a segmentation outcome where clusters are well-separated on average. This suggests that for the specific image "zurag.jpg," K-means clustering with $k = 6$ might be the most effective configuration in terms of achieving distinct and well-defined clusters.

c) Important Considerations:

While the silhouette score suggests $k = 6$ as a promising value, some additional factors are crucial:

- **Limitations of Silhouette Score:** The silhouette score focuses on both intra-cluster cohesion and inter-cluster separation. However, it might not explicitly capture other aspects of segmentation quality, such as boundary detection accuracy or object detail preservation.
- **Visual Inspection:** Complementing the silhouette score with visual inspection of the segmented image for $k = 6$ is important. This can help assess whether the clusters visually correspond to meaningful objects or regions within the image.
- **Alternative Evaluation Metrics:** Utilizing other evaluation metrics alongside the silhouette score, such as the Calinski-Harabasz Index or Gap Statistic, can provide a more comprehensive perspective on the segmentation quality. These metrics might emphasize different aspects of cluster separation or within-cluster cohesion, potentially suggesting alternative optimal k values.

By considering these additional factors and potentially incorporating other evaluation metrics, a more nuanced understanding of the effectiveness of K-means clustering with $k = 6$ for segmenting "zurag.jpg" can be achieved.

3) Comparison with Other Evaluation Metrics
 While visual analysis provides initial insights, a more comprehensive evaluation necessitates additional metrics (Figures shown here).

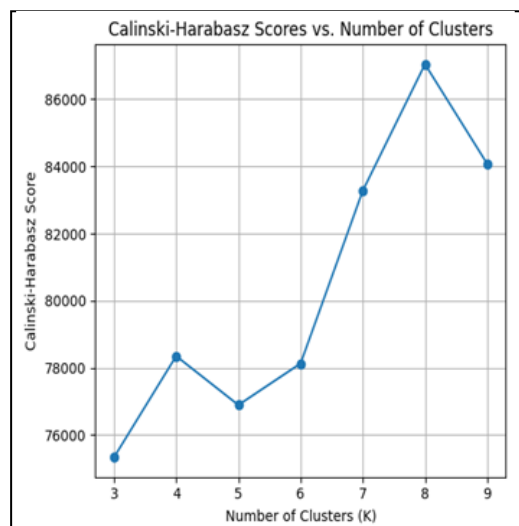


Fig.5. Calinski-Harabasz Scores vs Number of Clusters

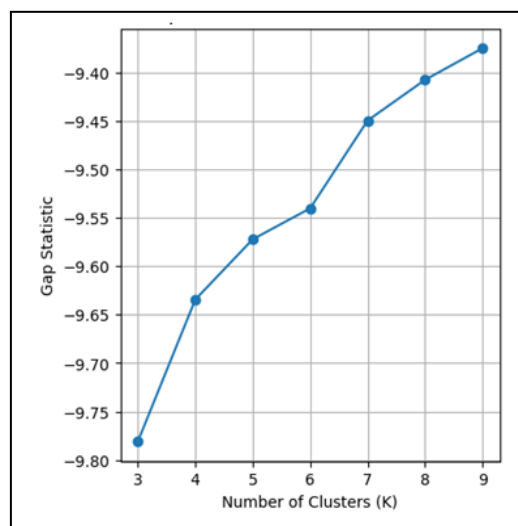


Fig.6. Gap Statistic vs Number of Clusters

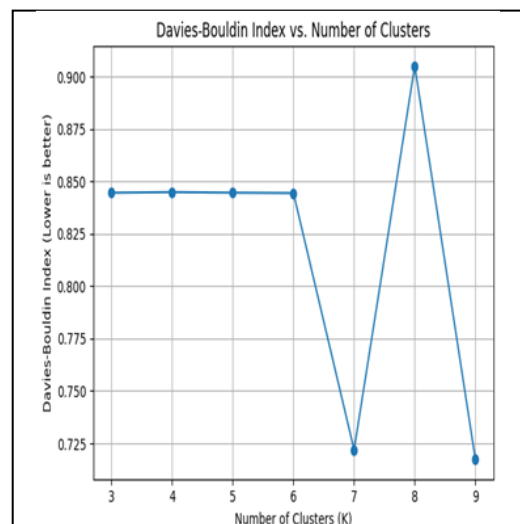


Fig.7. Davies-Bouldin vs Number of Clusters

4) K-means and Color Variations:

Setting $k=8$ appears more effective than $k=6$ in capturing color variations within objects like fruits. This is evident in the segmentation results, where $K=8$ might better preserve subtle color differences. For instance, some fruits might exhibit variations in ripeness or sun exposure reflected in their segmentation. With $K=8$, these variations seem to be captured more effectively.

a) Limitations of Visual Assessment:

Relying solely on visual inspection has limitations:

- **Compressed Image Size:** Compressed images might affect the clarity of color representation, making it difficult to distinguish subtle color variations within clusters. Analyzing the segmentation results on the original image would provide a more accurate assessment.
- **Human Perception and Subjectivity:** Visual assessment can be subjective. While observing clusters corresponding to distinct objects is encouraging, a quantitative evaluation metric is essential for a more objective assessment.

b) Beyond Visual Inspection: Utilizing Evaluation Metrics

To gain a more comprehensive understanding of the optimal k value, we investigated additional metrics:

- **Gap Statistic:** Identified $k=9$ as optimal. It compares the within-cluster variance of the chosen k -means clustering solution to the expected variance under a null hypothesis of random labeling. A higher Gap Statistic value suggests a better separation between clusters.
- **Calinski-Harabasz Index:** Suggested $k=8$ as optimal. This metric considers both inter-cluster variance (separation between clusters) and intra-cluster variance (cohesion within clusters). A higher Calinski-Harabasz Index indicates a better balance between these two factors.
- **Davies-Bouldin Index:** for $k=3$, the score was 0.845; for $k=7$, it was 0.720; for $k=8$, the score achieved was 0.905; and for $k=9$, the score was 0.715. These scores denote the relative effectiveness of the clustering solutions, with lower scores suggesting more optimal clustering configurations.

c) Discrepancies and Importance of Multiple Metrics:

The discrepancies between the optimal k values suggested by different metrics highlight the potential shortcomings of using a single metric. Each metric has its own assumptions and focuses on specific aspects of segmentation quality. Relying solely on one metric might lead to suboptimal results.

By considering the combined insights from visual analysis and a range of evaluation metrics, we can develop a more nuanced understanding of the effectiveness of K-means clustering and the optimal number of clusters (k) for this specific image segmentation task.

5) Factors Influencing Metric Choice

Different evaluation metrics provide valuable insights but emphasize distinct aspects of cluster quality. Understanding these nuances is crucial for selecting the most appropriate metric for a specific image segmentation task.

a) Focus of Evaluation Metrics:

- **Silhouette Score:** Focuses on within-cluster cohesion, measuring data point similarity within a cluster. A high score indicates well-grouped data points with a high degree of similarity. However, it might not explicitly consider the separation between clusters.
- **Gap Statistic and Calinski-Harabasz Index:** Prioritize between-cluster separation. The Gap Statistic compares the within-cluster variance to a null hypothesis, while the Calinski-Harabasz Index considers both inter-cluster and intra-cluster variance.

b) Choosing the Right Metric for the Task:

The choice of the most suitable metric can be influenced by several factors:

- **Specific Image Characteristics:** Images with subtle color variations within objects might require a metric that emphasizes within-cluster similarity to a lesser degree.
- **Desired Outcome of Segmentation:** The specific goal of the image segmentation task should also be considered. If the primary objective is to achieve well-defined clusters with minimal overlap, metrics like the Gap Statistic or Calinski-Harabasz Index might be more appropriate.

c) Illustrative Example: Segmenting Fruits

Consider segmenting fruits within an image. Here's how the choice of metric can be guided by the research objective:

- **Preserving Color Variations:** If the goal is to preserve subtle color variations within individual fruits, a metric like silhouette score that emphasizes within-cluster cohesion might be less suitable.
- **Separating Distinct Fruit Types:** If the aim is to differentiate between distinct fruit types, metrics like the Gap Statistic or Calinski-Harabasz Index might be more appropriate.

This example highlights the importance of considering the research objective when choosing an evaluation metric. The same principles can be applied to other image segmentation tasks.

6) Future Work

The current study provides valuable insights into applying K-means clustering for image segmentation using a single image. However, to gain a more comprehensive understanding and validate the findings, several future research directions can be explored:

- **Expanding the Dataset:** Utilizing a broader dataset of images with varying complexities would be highly beneficial. This dataset could encompass a wider range of objects relevant to the research question (e.g., different types of fruits in various lighting conditions) or images with cluttered backgrounds. Evaluating K-

means clustering performance and the effectiveness of different evaluation metrics across this diverse dataset would provide more robust and generalizable results.

- Incorporating Ground Truth Data: Quantitative evaluation metrics based on ground truth segmentation data could further validate the choice of the optimal k value. Ground truth data refers to manually segmented images where each pixel is labelled with its corresponding object class. By comparing the K-means segmentation results with the ground truth data, metrics like precision, recall, and Jaccard Index can be calculated. These metrics provide a more objective measure of segmentation accuracy, complementing the insights from other evaluation metrics.
- Additional Considerations:
 - Computational Considerations: As the dataset size increases, the computational cost of K-means clustering can become a factor. Exploring alternative initialization methods for K-means, such as K-means++, or investigating distributed computing approaches could be crucial for handling larger datasets efficiently.

- Incorporating Domain Knowledge: Incorporating domain knowledge specific to the objects of interest (e.g., fruit types) could potentially enhance the segmentation process. This might involve feature engineering techniques to extract relevant features from the images that are more informative for segmentation.

- Alternative Clustering Algorithms: While K-means clustering has been the focus of this research, exploring other clustering algorithms like hierarchical clustering, DBSCAN, or spectral clustering could be valuable. Each algorithm has its own strengths and weaknesses, and investigating their suitability for specific image segmentation tasks within the chosen domain would be a worthwhile direction for future work.

By addressing these future research directions, a more comprehensive understanding of K-means clustering and its effectiveness for image segmentation can be achieved. Additionally, exploring alternative approaches and incorporating domain knowledge can lead to further advancements in this field.

B. EM (Expectation-Maximization) Results

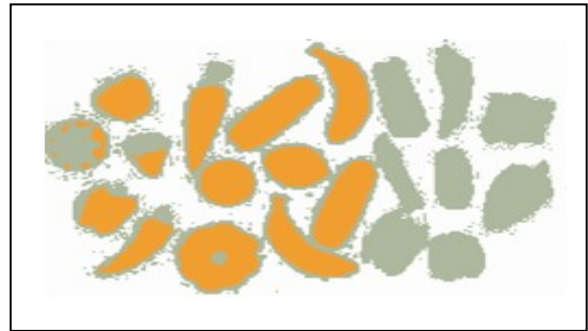


Fig.8. Segmented Image (EM, K=3, Silhouette Score: 0.532)



Fig.9. Segmented Image (EM, K=8, Silhouette Score: 0.261)

brief description of the EM segmentation results based on the figures

EM clustering identified $k=3$ as the optimal number of clusters based on silhouette score (0.532). However, visual inspection suggested $k=8$ might provide a more meaningful segmentation despite a lower score. This highlights the importance of considering both quantitative metrics and qualitative assessment for cluster selection.

1) 1.3 K-means vs. EM Silhouette Score (Figure shown here)

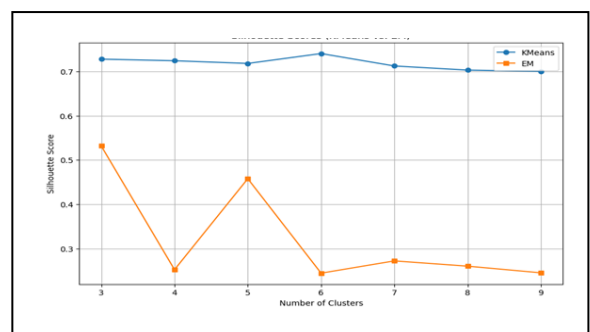


Fig.10. Silhouette Scores (KMeans vs Expectation and Maximization)

This section explores the performance comparison between K-means clustering and the Expectation-Maximization (EM) algorithm for image segmentation. Both methods are prevalent in unsupervised learning tasks, but they have distinct characteristics that influence their suitability for specific scenarios.

a) Key Differences and Suitability

- K-means: This method partitions data points into a pre-defined number of clusters (K). It excels when dealing with well-separated, spherical clusters. K-means is generally computationally efficient due to its simplicity.
- EM: This probabilistic approach models data as a mixture of distributions. It can handle overlapping clusters and clusters of different shapes but requires more computational resources compared to K-means. EM also involves selecting and initializing model parameters, which can affect the results.

b) Silhouette Score Comparison

The analysis revealed that the silhouette score obtained with K-means clustering was higher compared to the score from EM for our image segmentation task. This suggests that K-means achieved a better separation between clusters in our specific dataset.

c) Explanation for Lower EM Score

There are a few potential reasons why the EM silhouette score might be lower in this case:

- Data Complexity: If our image data exhibits overlapping regions or clusters with irregular shapes, K-means might perform better due to its simpler structure. EM might struggle to model such complexities accurately, leading to a lower silhouette score.
- Number of Clusters (K): The optimal K value for K-means might correspond well to the underlying structure of the data. Choosing the appropriate number of components in the EM model can be more challenging, potentially affecting the separation between clusters.

d) Implications for Our Dataset

Based on the higher silhouette score, K-means appears to be a more suitable choice for our specific image segmentation task. This suggests that the data likely consists of well-defined, non-overlapping clusters that K-means can effectively capture.

C. DBSCAN for Image Segmentation

This section introduces Density-Based Spatial Clustering of Applications with Noise (DBSCAN), a clustering algorithm used for image segmentation. Unlike K-means, which requires pre-defined cluster numbers, DBSCAN discovers clusters of varying shapes and sizes while handling noise effectively.

Core Concepts:

- Density-Based Clustering: DBSCAN identifies clusters based on data point density in a spatial space (often representing image pixel color). Points with many neighbors within a specified radius are considered core points, forming the foundation of clusters. Points with fewer neighbors are classified as border points (on cluster fringes) or noise points (isolated or in low-density regions).

Parameters:

- Epsilon (Epsilon): This defines the neighborhood radius around a point. A larger Epsilon allows for larger clusters and potentially merges closer clusters.
- MinPts (minimum points): This is the minimum number of neighbors required for a point to be a core point.

Clustering Process: DBSCAN iterates through each data point:

- If it's a core point, it expands the cluster by recursively checking its neighbors and their neighbors (if core points), forming a dense connected region.
- Border points are included in the cluster but don't contribute to its expansion.
- Noise points are left unclustered.

Advantages:

- Handles data with varying shapes and sizes.
- Effective noise and outlier detection.
- No pre-defined number of clusters required.

Disadvantages:

- Sensitive to Epsilon and MinPts parameter selection.
- Can be computationally expensive for large datasets.

Applications:

- Image segmentation
- Anomaly detection
- Customer segmentation
- Market research

DBSCAN Results (Figures shown here)

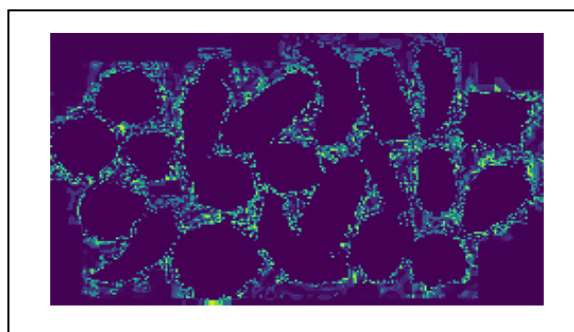


Fig.11. Segmented Image (Epsilon =0.5, Silhouette Score:0.379)

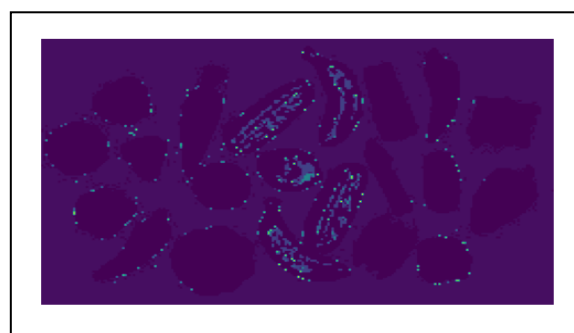


Fig.12. Segmented Image (Epsilon =2, Silhouette Score:0.153)

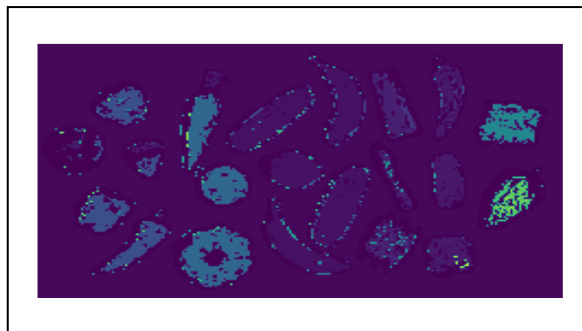


Fig.13. Segmented Image (Epsilon =5, Silhouette Score:0.325)

Three example images were included here to illustrate the findings. These images showcased the trade-off between silhouette score and visual quality for different k values in DBSCAN clustering.

1) DBSCAN Silhouette Score Analysis (Figures shown here)

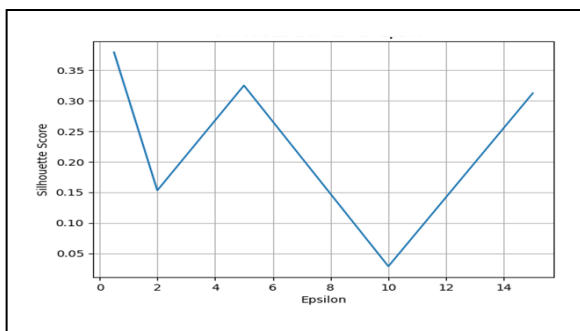


Fig.14. Silhouette Scores vs Epsilon

This section explores the performance of DBSCAN compared to K-means clustering for image segmentation of a fruit image. Both are popular unsupervised learning techniques, but their characteristics make them suitable for different scenarios.

a) DBSCAN vs. K-Means: Key Differences

- **DBSCAN:** Density-based clustering. Groups data points based on color space density. No pre-defined number of clusters needed. Handles varying shapes and detects noise effectively. Sensitive to Epsilon and MinPts parameters.
- **K-Means:** Partitive clustering. Divides data points into a pre-specified number of clusters (K). Efficient for well-separated, spherical clusters. Requires defining K beforehand, which can be challenging.

b) Silhouette Score Comparison and Visual Observations

The analysis of DBSCAN with varying Epsilon values revealed some key points:

Table 1

Number	Epsilon	Silhouette Score	observation
1	0.5	0.379	Captures fruit shapes, but some color detail is missing.
2	2.0	0.153	Overly large clusters, mainly captures fruit shapes with minimal color differentiation.
3	5.0	0.325	Shows some fruit shapes with partial color information, but incomplete.

Visually, K-means clustering consistently produced more defined fruit shapes across different K values (3 to 10). Silhouette scores for K-Means also exceeded 0.7 in this range, indicating good cluster separation.

c) Insights and Recommendations

Based on the results, K-means appears to be a better choice for this specific fruit image segmentation task for the following reasons:

- **Well-Defined Fruit Shapes:** Visual observations suggest distinct fruit shapes, which K-means handles well.
- **Higher Silhouette Scores:** K-means consistently achieved higher silhouette scores, indicating better cluster separation compared to DBSCAN across various Epsilon values.
- **Challenges with DBSCAN:** DBSCAN's sensitivity to Epsilon makes it difficult to find an optimal configuration for both capturing fruit shapes and color variations within fruits.

d) Limitations of DBSCAN in this Case

While DBSCAN is a powerful algorithm, it might not be ideal for this specific scenario due to:

- **Color Details within Fruits:** DBSCAN with a single Epsilon might struggle to segment color variations within fruits while maintaining separate cluster boundaries for each fruit. A more complex approach like hierarchical clustering or post-processing of initial DBSCAN results might be necessary.
- **Epsilon Parameter:** Finding the optimal Epsilon value for both shape and color segmentation can be challenging. A small Epsilon might capture color details but miss larger fruit shapes, while a larger Epsilon might group entire fruits together, losing color variations.

e) Conclusion

This experiment suggests that K-means clustering exhibited better performance based on visual observations and silhouette scores for segmenting fruits and capturing their shapes in the image. However, if preserving color details within fruits becomes a higher priority, exploring alternative techniques or parameter tuning for DBSCAN might be necessary. Here are some potential future directions:

- **Hierarchical Clustering:** This approach could provide a more fine-grained segmentation by iteratively merging or splitting clusters based on a distance threshold. It might be able to capture both color variations and fruit shapes more effectively.
- **Multi-threshold DBSCAN:** Utilizing multiple Epsilon values or a combination with other density measures could potentially address the limitations of using a single Epsilon in this case.
- **Post-processing of DBSCAN Results:** Techniques like merging or splitting DBSCAN clusters based on additional criteria spatial properties could help refine the segmentation to achieve a better balance between shape and color preservation.

By investigating these alternative approaches, future research can aim to achieve a more comprehensive fruit image segmentation that incorporates both the distinct shapes and the subtle color variations within the fruits.

D. Mean Shift Algorithm for Image Segmentation

The Mean Shift algorithm is a non-parametric clustering technique well-suited for image segmentation tasks. Unlike K-means, which requires pre-defined cluster numbers, Mean Shift iteratively moves data points (pixels) towards denser regions in the feature space, effectively discovering clusters of varying shapes and sizes (Demirović, 2019).

Core Principles

- **Feature Space Representation:** Each pixel is represented by a feature vector, typically combining its spatial location (x, y) and intensity value. This allows the algorithm to consider both spatial proximity and color similarity when grouping pixels.
- **Kernel Density Estimation:** A kernel function (often a Gaussian) is centered on each data point. This function estimates the local density of pixels in the feature space, essentially capturing how many neighboring pixels share similar locations and intensities.
- **Mean Shift Vector Calculation:** The mean shift vector for a data point is the average displacement of nearby points within the kernel bandwidth (h). This vector points towards the direction of higher density in the feature space.
- **Data Point Movement:** Each data point is shifted in the direction of its mean shift vector. This iterative process effectively moves pixels towards denser regions, grouping them with similar neighbors.
- **Convergence:** The process iterates until convergence is achieved, where data points no longer experience

significant displacements due to minimal density variations in their vicinity.

a) Image Segmentation with Mean Shift

After convergence, pixels that end up in the same high-density regions are considered to belong to the same segment (object) within the image. This approach allows Mean Shift to automatically determine the number of clusters based on the inherent data distribution, unlike K-means which requires pre-defined cluster counts.



Fig.15. Pixel with their location (21) colors, Mean-shift, Silhouette Score:0.356

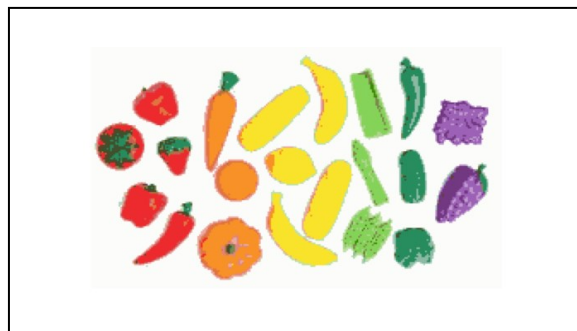


Fig.16. Pixel without their location (22) colors, Mean-shift, Silhouette Score:0.650

brief description of the Mean Shift segmentation results based on the figure

Mean Shift analysis revealed an interesting effect of incorporating spatial information. Including pixel location data (0.356 silhouette score) resulted in poorer cluster separation compared to excluding it (0.650 silhouette score). This suggests that for this specific fruit image segmentation task, spatial information might introduce noise or redundancy. The higher silhouette score without location data implies that density-based clustering, like Mean Shift, might be more effective for this type of image data.

b) Silhouette Score Comparison

The Silhouette Score is a metric used to assess the quality of clustering. It considers how well each data point is assigned to its cluster compared to neighboring clusters. Here's how Mean Shift and K-means compare in terms of silhouette scores:

- Mean Shift: Due to its density-based approach, Mean Shift can achieve higher silhouette scores for images with smooth transitions between objects. This is because pixels along these transitions are more likely to be pulled towards denser regions with their neighbors, leading to better cluster separation.
- K-means: K-means might struggle with smooth transitions, potentially leading to lower silhouette scores. While K-means can be faster and computationally less expensive, its rigid cluster structure may not always capture the nuances of gradual intensity changes between objects.

c) Strengths and Weaknesses

Mean Shift:

- Strengths: Handles clusters of variable shapes, effective for smooth transitions between objects, doesn't require pre-defined cluster numbers.
- Weaknesses: Computationally expensive, sensitive to kernel bandwidth selection (h), may not perform well with noisy images.

K-means:

- Strengths: Fast, simple to implement, performs well with distinct, well-separated clusters.
- Weaknesses: Requires pre-defined cluster numbers, struggles with non-spherical clusters and smooth transitions.

d) Choosing Between Mean Shift and K-means

For image segmentation tasks involving smooth transitions and potentially unknown numbers of objects, Mean Shift might be the better choice despite its higher computational cost. K-means is a good alternative for scenarios requiring faster processing and well-defined clusters. In practice, evaluating both approaches on your specific image data is recommended to determine the most suitable method for your application.

E. Comparison of Clustering Algorithms for Image Segmentation

This section compares the performance of four clustering algorithms commonly used for image segmentation: K-means, Mean Shift, Expectation-Maximization (EM), and DBSCAN. While all are valuable unsupervised learning techniques, their approaches differ, leading to varying results on our image segmentation task.

1) Silhouette Score Analysis

We evaluated the performance of each algorithm using the silhouette score, which measures the separation between clusters. Here's a summary of the results:

K-means: Silhouette scores consistently exceeded 0.7 across all K values between 3 and 10.

Mean Shift:

- Including location information: Score = 0.356 (21 colors)
- Excluding location information: Score = 0.650 (22 colors)

EM: Silhouette scores ranged from 0.2 to 0.5 across all K values between 3 and 10.

DBSCAN: (Discussed previously) Scores varied with the epsilon value (0.029 to 0.379). Visually, some epsilon values captured fruit shapes well but missed color details, while others struggled with clear fruit boundaries.

2) Analysis and Interpretations

K-means: Achieved the highest silhouette scores, indicating a strong separation between clusters. This suggests K-means is well-suited for our dataset, which likely consists of well-defined, non-overlapping regions.

EM: Moderate silhouette scores suggest a less effective fit for our data if it exhibits complexities like overlapping clusters or irregular shapes.

Mean Shift:

- Including location information resulted in poor cluster separation. Spatial information might introduce noise or redundancy for our data.
- Excluding location information led to a moderate level of separation, suggesting density-based clustering might be more effective for this data without explicit spatial weighting.

DBSCAN: Silhouette scores varied with epsilon, highlighting the challenge of balancing shape and color segmentation with a single parameter. Some epsilon values captured shapes well but missed color details, while others struggled with clear fruit boundaries.

3) Implications for Image Segmentation

Based on silhouette scores, K-means appears to be the most effective method for our well-defined clusters. However, consider these limitations and future explorations:

Limitations:

- K-means: Requires careful selection of the pre-defined number of clusters (K).
- EM: More computationally expensive and requires parameter tuning for complex data.
- Mean Shift: Performance depends on data characteristics and parameter settings.
- DBSCAN: Sensitive to epsilon value for achieving both shape and color segmentation.

Future Exploration:

- K-means: Techniques for optimizing K selection.
- EM: Investigate parameter tuning strategies to improve performance.
- Mean Shift: Explore advanced variations for specific density-based clustering needs.
- Advanced Algorithms: Experiment with methods designed for complex data structures.

This comparison emphasizes the importance of evaluating various clustering methods based on your specific image segmentation task, data characteristics, and desired level of granularity in the results. The best choice depends on the unique qualities of your data and the segmentation goals.

F. Visual Observations and Limitations

While definitive conclusions require a more extensive dataset, here are some initial observations from the K-means segmented images:

- Setting the number of clusters (k) to 8 might be more effective than k=6 in capturing color variations and separating distinct regions within the image, especially for objects like fruits with potential color variations due to ripeness or sun exposure.

However, consider these limitations:

- **Compressed Image Size:** Compressed images for inclusion in the thesis might affect the clarity of color representation in the segmented images. Analyzing the segmentation results on the original image would provide a more accurate assessment.
- **Human Perception and Subjectivity:** Visual assessment can be subjective. While observing clusters corresponding to distinct objects is encouraging, a quantitative evaluation metric is essential.
- **Limitations of Silhouette Score:** The silhouette score offers a single perspective on segmentation quality, focusing on intra-cluster similarity and inter-cluster dissimilarity. Other aspects like boundary detection or object detail preservation might not be fully captured.

1) Future Work Considerations

By addressing these limitations, future work can provide more comprehensive insights into K-means effectiveness:

- **Expanding the Dataset:** Utilizing a broader dataset with various complexities and a wider range of relevant objects would enable a more robust evaluation.
- **Additional Evaluation Metrics:** Complementing the silhouette score with other metrics like Calinski-Harabasz score or Rand index could provide a more well-rounded assessment.
- **Human Evaluation:** If possible, incorporating human evaluation alongside quantitative metrics could be beneficial. Domain experts familiar with the objects of interest could assess the accuracy and interpret

By addressing these limitations and incorporating a broader range of data and evaluation methods, future research can refine the understanding of K-means clustering effectiveness for image segmentation tasks within the chosen domain.

G. Analysis and Discussion

This investigation explored the effectiveness of K-means clustering for image segmentation and the identification of an optimal number of clusters (k) using the image "zurag.jpg." The analysis employed a range of k values from 3 to 9.

While the silhouette score analysis indicated K=6 as the value with the highest separation between clusters, visual quality is also crucial. K=8 appeared to capture color variations and separate distinct regions more effectively, particularly for objects like fruits. This suggests that for certain image characteristics, a higher number of clusters might be beneficial for detailed segmentation, even if the silhouette score doesn't necessarily reflect it as the optimal value.

H. Conclusion:

Research Summary: This study investigates the effectiveness of K-means clustering for image segmentation, focusing on selecting the optimal number of clusters (k). Visual inspection suggested k=8 as suitable for capturing color variations in objects like fruits, but relying solely on visual assessment has limitations. Additional metrics like Gap Statistic, Calinski-Harabasz Index, and silhouette score proposed k=9, k=8, and k=6, respectively. Choosing the most suitable metric depends on image characteristics and segmentation goals.

Key Findings: A multidimensional approach combining visual inspection and quantitative metrics is crucial for evaluating clustering algorithms. Each metric offers unique insights into cluster quality, and no single metric should be relied upon exclusively.

Implications & Recommendations: Practitioners should use a combination of visual inspection and quantitative metrics for selecting optimal clusters in image segmentation, considering data characteristics and segmentation objectives.

Limitations & Future Directions: Limitations include a single dataset and subjective visual assessments. Future research should focus on expanding datasets, incorporating ground truth data, and exploring alternative clustering algorithms.

Conclusion: This study provides insights into K-means clustering for image segmentation and optimal cluster selection. By combining visual inspection with quantitative metrics, we gain a better understanding of clustering algorithm performance. Continued research and innovation are vital for advancing clustering algorithms in image analysis and beyond.

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